



## Grade 9 - Mathematics

### Organising and Representing Data 4



### Memo

1. The table represents examination percentages obtained by a Grade 9 class

|    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|
| 30 | 26 | 41 | 95 | 54 | 36 | 16 | 26 | 31 | 39 |
| 47 | 71 | 42 | 51 | 35 | 33 | 33 | 41 | 15 | 29 |
| 55 | 63 | 29 | 28 | 81 | 52 | 45 | 42 | 28 |    |

- Order the data
- Find the median
- Find  $Q_1$ .
- Find  $Q_3$
- Determine the interquartile range.
- Determine whether the data is bunched or dispersed.
- State the outliers, if any.
- Divide the data into classes of 10% ranges.
- Draw up a frequency table.
- Determine the modal class.
- Use the frequency table to calculate the estimated mean.

a. 15; 16; 26; 26; 28; 28; 29; 29; 30; 31; 33; 33; 35; 36; 39; 41; 41; 42; 42; 45; 47; 51; 52; 54; 63; 71; 81; 95

b. 
$$\frac{n+1}{2}$$
$$= \frac{29+1}{2}$$
$$= \frac{30}{2}$$
$$= 15^{\text{th}} \text{ value}$$

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c. 
$$Q_1 = \frac{n+1}{4}$$
$$= \frac{30}{4}$$
$$= 7,5$$

Between 7<sup>th</sup> and 8<sup>th</sup> value  
Between 29 and 29 = 29



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$$\begin{aligned} \text{d. } Q_3 &= \frac{3(n+1)}{4} \\ &= \frac{90}{4} \\ &= 22,5 \end{aligned}$$

Between 22<sup>nd</sup> and 23<sup>rd</sup> value  
Between 51 and 52 = 51,5

$$\begin{aligned} \text{e. } Q_3 - Q_1 & \\ &= 51,5 - 29 \\ &= 22,5 \end{aligned}$$

$$\begin{aligned} \text{f. } Q_1 - (1,5 \times \text{IQR}) & \\ &= 29 - (1,5 \times 22,5) \\ &= 29 - 33,75 \\ &= - 4,75 \end{aligned}$$

$$\begin{aligned} Q_3 + (1,5 \times \text{IQR}) & \\ &= 51,5 + (1,5 \times 22,5) \\ &= 51,5 + 33,75 \\ &= 85,25 \end{aligned}$$

The data to the left of the median is bunched but to the right of the median it is dispersed.

- g. There is one outlier, which is the value of 95
- h. The data classes would be 0-10; 11-20; 21-30; 31-40; 41-50; 51-60; 61-70; 71-80; 81-90; 91-100.
- i. Frequency table

| Class interval | Frequency |
|----------------|-----------|
| 0 – 10         | 0         |
| 11 – 20        | 2         |
| 21 – 30        | 7         |
| 31 – 39        | 6         |
| 41 – 50        | 6         |
| 51 – 59        | 3         |
| 60 – 69        | 1         |
| 70 - 79        | 1         |
| 80 – 89        | 1         |
| 90 - 100       | 1         |

- j. The modal class is the 21 – 30 data class



k. Frequency table

| Class interval | Frequency | Midpoint | Freq x Midpoint |
|----------------|-----------|----------|-----------------|
| 1 – 10         | 0         | 5,5      | 0               |
| 11 – 20        | 2         | 15,5     | 31              |
| 21 – 30        | 7         | 25,5     | 178,5           |
| 31 – 39        | 6         | 35,5     | 213             |
| 41 – 50        | 6         | 45,5     | 273             |
| 51 – 59        | 3         | 55,5     | 166,5           |
| 60 – 69        | 1         | 65,5     | 65,5            |
| 70 - 79        | 1         | 75,5     | 75,5            |
| 80 – 89        | 1         | 85,5     | 85,5            |
| 90 - 100       | 1         | 95,5     | 95,5            |

$$\begin{aligned}\text{Estimated mean} &= \text{sum of } fx \div \text{number of values} \\ &= 1184 \div 29 \\ &= 40,8\end{aligned}$$

l. The modal class is 0 – 29

m. Estimated Mean

| Class interval | Frequency | Midpoint | Freq x Midpoint |
|----------------|-----------|----------|-----------------|
| 0 - 29         | 33        | 14,5     | 478,5           |



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|           |    |       |        |
|-----------|----|-------|--------|
| 30 – 49   | 8  | 39,5  | 316    |
| 50 - 69   | 17 | 59,5  | 1011,5 |
| 70 – 89   | 12 | 79,5  | 954    |
| 90 – 109  | 15 | 99,5  | 1492,5 |
| 110 – 129 | 10 | 119,5 | 1195   |
| 130 – 149 | 5  | 139,5 | 697,5  |
| 150 – 169 | 2  | 159,5 | 319    |
| 170 - 189 | 2  | 179,5 | 359    |

Add all  $fx$  values

$$488,5 + 316 + 1011,5 + 954 + 1492,5 + 1195 + 697,5 + 319 + 359 \\ = 6833$$

Divide by total number of elements in the data: (104)

$$6833 \div 104 = 65,7\text{cm}$$

$$\begin{aligned} \text{n. Median} &= \frac{n+1}{2} \\ &= \frac{104+1}{2} \\ &= \frac{105}{2} \\ &= 52,5 \end{aligned}$$

The median is between the 52<sup>nd</sup> and 53<sup>rd</sup> value. It will be in the 50 – 69 range. It can be estimated as being 59,5.

- o. The mode will probably be in the 0 – 29 class due to it having the highest frequency but due to the fact that no individual readings are given it would be impossible to determine the actual mode.